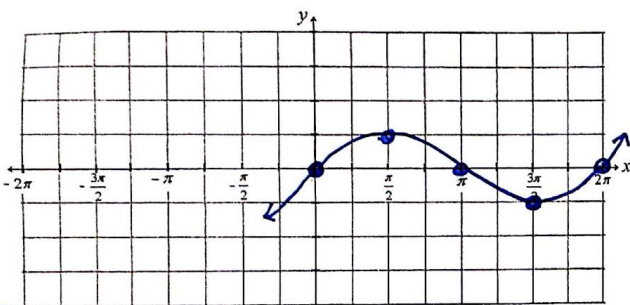


$$y = a \cdot \sin [b(x-c)] + d$$

$$y = a \cdot \cos [b(x-c)] + d$$

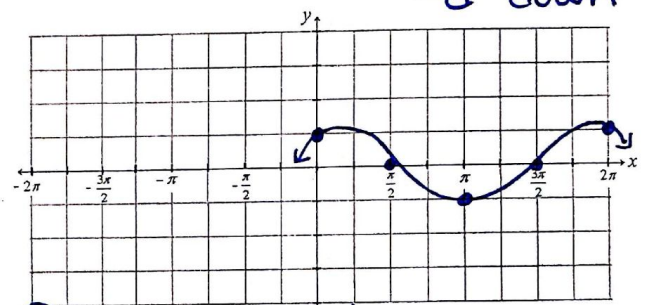
$|a|$ = amplitude $+c$ left
 $-c$ right
 $\frac{2\pi}{b}$ = period $+d$ up
 $-d$ down



① $y = \sin x$
SOIL

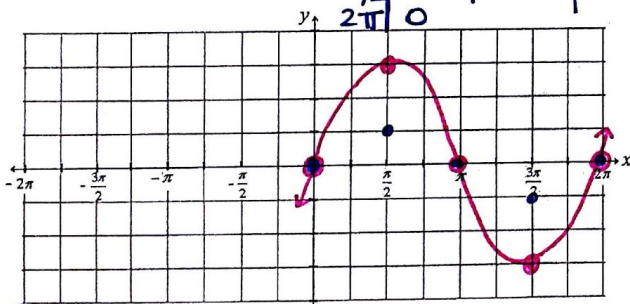
x	y
0	0
$\pi/2$	1
π	0
$3\pi/2$	-1
2π	0

amp = 1
per = $\frac{2\pi}{1}$



② $y = \cos x$
clouds

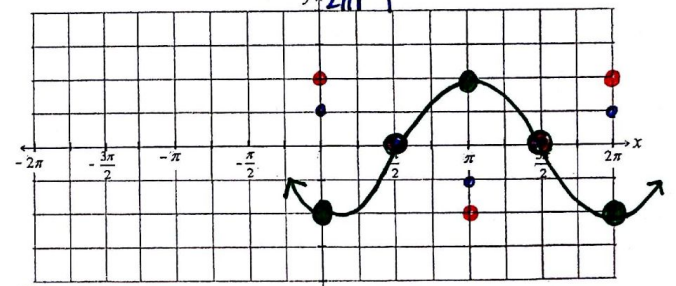
x	y
0	1
$\pi/2$	0
π	-1
$3\pi/2$	0
2π	1



③ $y = 3 \sin x$

MathBits.com

amp = 3
per = $\frac{2\pi}{1} = 2\pi$

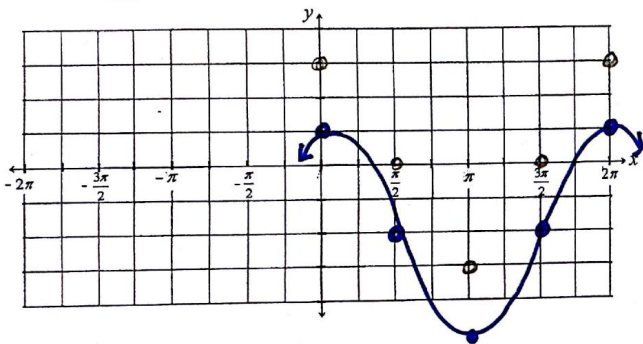


④ $y = -2 \cos x$

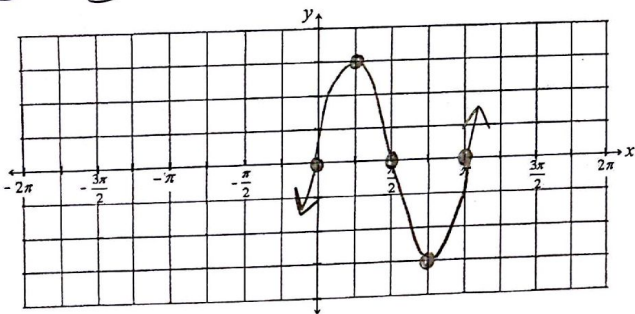
MathBits.com

amp = 2
per = $\frac{2\pi}{1} = 2\pi$
reflects x-axis

⑦ $y = 3\cos x - 2$

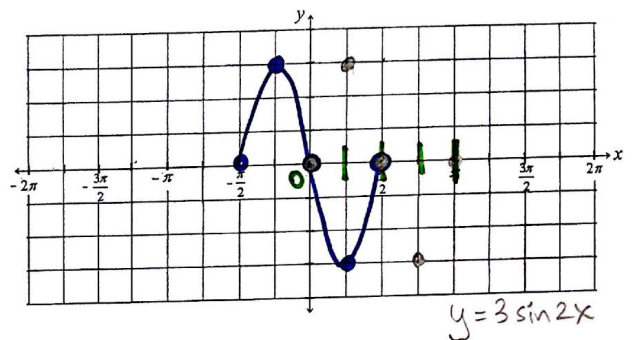


⑤ $y = 3\sin(2x)$

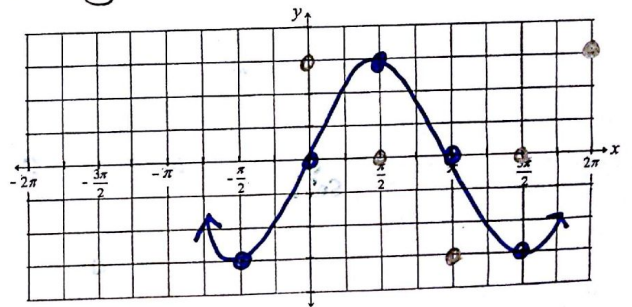


$per = \frac{2\pi}{2} = \pi$
MathBits.com

⑧ $y = 3\sin(2x + \pi)$ $per = \frac{2\pi}{2} = \pi$
 $y = 3\sin 2(x + \frac{\pi}{2})$



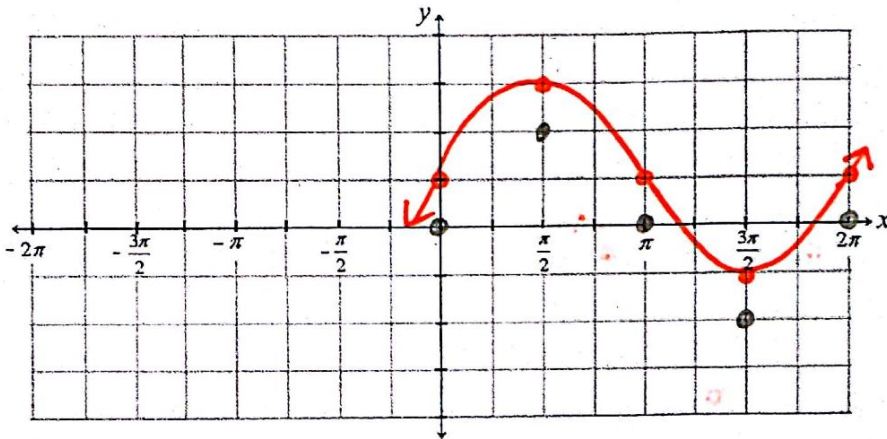
⑥ $y = 3\cos(x + \frac{\pi}{2})$



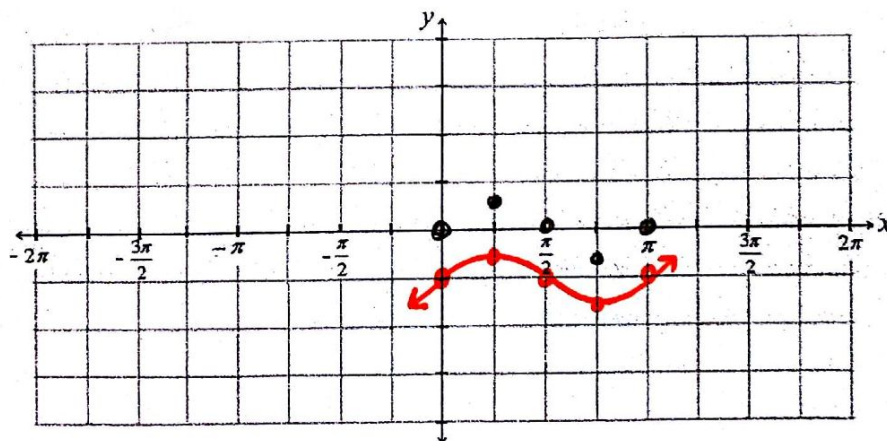
$per = \frac{2\pi}{1}$
MathBits.com

Graphing Sine Functions -

$y = 2\sin(x) + 1$ $2\sin x$
 Amplitude = 2 Period = 2π Phase shift = none Vertical Shift = up 1
 Find the 5 key points. Divide the period by 4 to get the quarter period. We start with the value of x where the cycle begins.
 $x_1 = 0$ $x_2 = \frac{\pi}{2}$ $x_3 = \pi$ $x_4 = \frac{3\pi}{2}$ $x_5 = 2\pi$
 $y_1 = 0$ $y_2 = 2$ $y_3 = 0$ $y_4 = -2$ $y_5 = 0$



$y = \frac{1}{2}\sin(2x) - 1$ $\frac{1}{2}\sin(2x)$
 Amplitude = $\frac{1}{2}$ Period = π Phase shift = none Vertical Shift = down 1
 Find the 5 key points. Divide the period by 4 to get the quarter period. We start with the value of x where the cycle begins.
 $x_1 = 0$ $x_2 = \frac{\pi}{4}$ $x_3 = \frac{\pi}{2}$ $x_4 = \frac{3\pi}{4}$ $x_5 = \pi$
 $y_1 = 0$ $y_2 = \frac{1}{2}$ $y_3 = 0$ $y_4 = -\frac{1}{2}$ $y_5 = 0$



Graphing Sine Functions - ~~Work~~work

Class

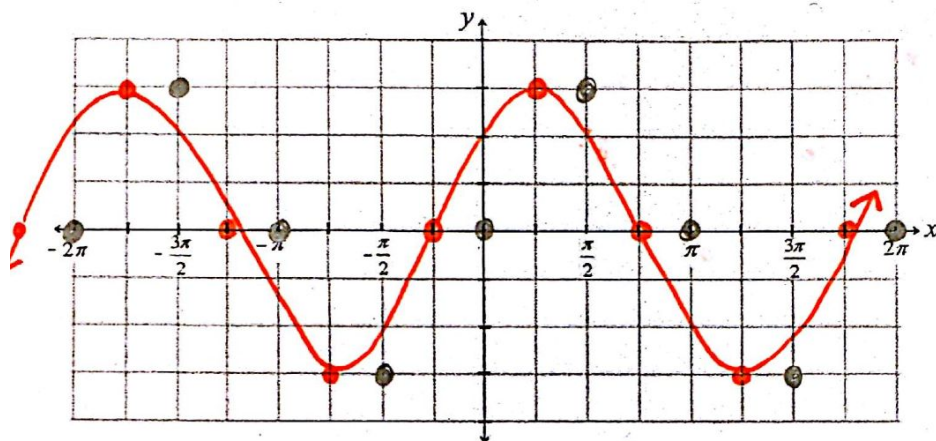
Key

$y = 3\sin\left(x + \frac{\pi}{4}\right)$ $3\sin x$

Amplitude = 3 Period = 2π Phase shift = left $\frac{\pi}{4}$ Vertical Shift = none

Find the 5 key points. Divide the period by 4 to get the quarter period. We start with the value of x where the cycle begins.

$x_1 = 0$	$x_2 = \frac{\pi}{2}$	$x_3 = \pi$	$x_4 = \frac{3\pi}{2}$	$x_5 = 2\pi$
$y_1 = 0$	$y_2 = 3$	$y_3 = 0$	$y_4 = -3$	$y_5 = 0$



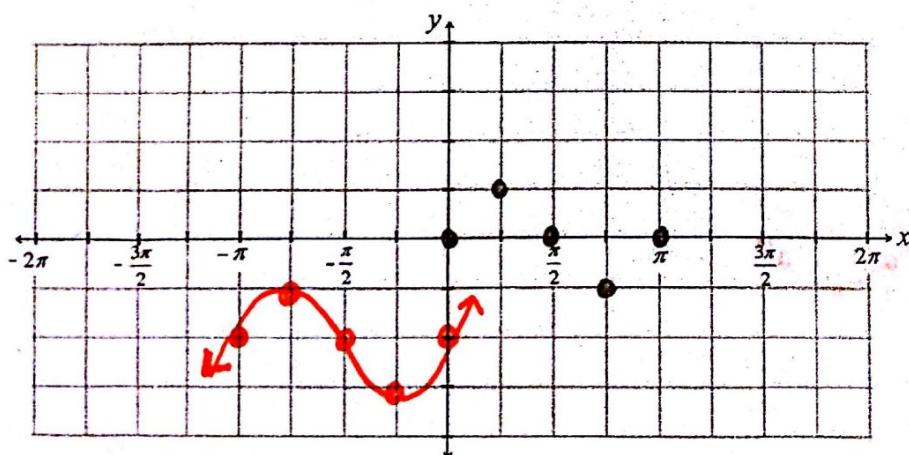
$y = \sin(2x)$

$y = \sin 2(x + \pi) - 2$

Amplitude = 1 Period = π Phase shift = left π Vertical Shift = down 2

Find the 5 key points. Divide the period by 4 to get the quarter period. We start with the value of x where the cycle begins.

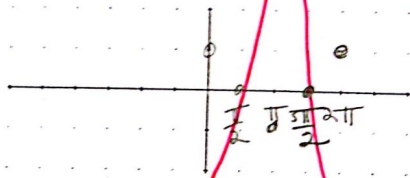
$x_1 = 0$	$x_2 = \frac{\pi}{4}$	$x_3 = \frac{\pi}{2}$	$x_4 = \frac{3\pi}{4}$	$x_5 = \pi$
$y_1 = 0$	$y_2 = 1$	$y_3 = 0$	$y_4 = -1$	$y_5 = 0$



Class KEY

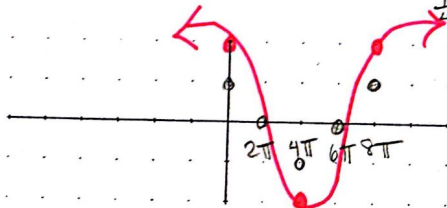
Graphing Cosine ~~work~~

1. $y = -3\cos x$ Amplitude: 3 Period: 2π



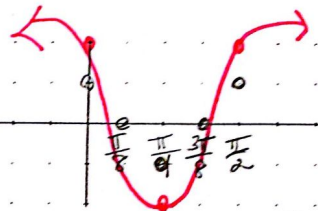
2.

$y = 2\cos\frac{1}{4}x$ Amplitude: 2 Period: $\frac{2\pi}{\frac{1}{4}} = 8\pi$

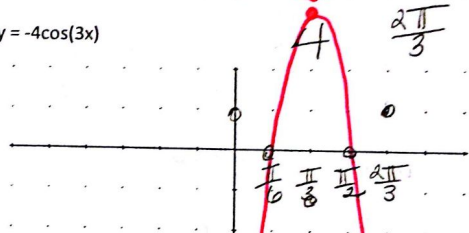


2 $\frac{2\pi}{4} = \frac{\pi}{2}$

3. $y = 2\cos(4x)$



4. $y = -4\cos(3x)$



5. Write the equation of the cosine graph $y = A\cos(Bx)$ given the following:

Amplitude: 2

Period: $\frac{\pi}{3}$



$$\frac{2\pi}{b} = \frac{\pi}{3}$$

$$\pi b = 6\pi$$

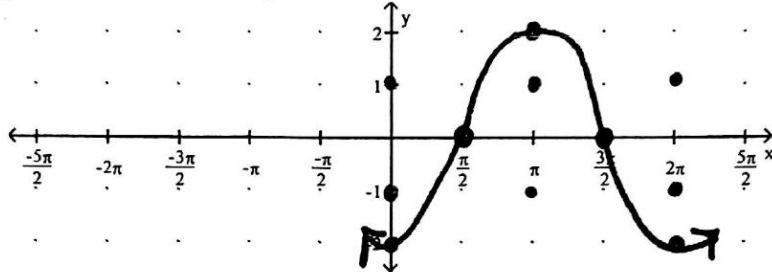
$$b = 6$$

$$y = 2\cos(6x)$$

Graphing Sine and Cosine Function Name Key

1) Graph the function.

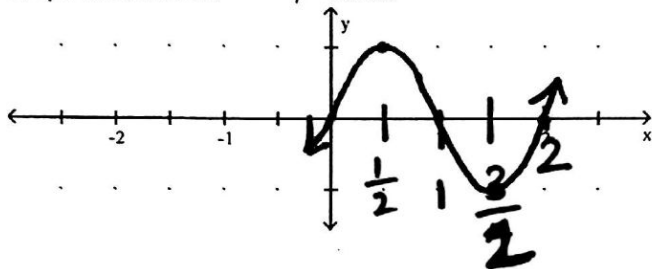
$y = -2 \cos x$



Amp: 2
 Period: 2π
 reflect over x-axis

2) Graph the function.

$y = \sin \pi x$



Amp: 1
 Period: $\frac{2\pi}{\pi} = 2$

3) Give the Amplitude and period of the function:

a) $y = \cos 3x$

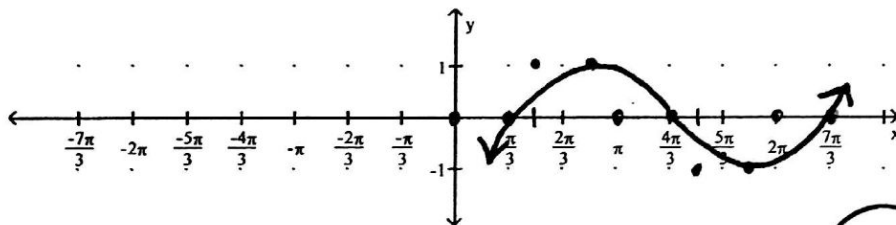
Amp: 1 Period: $\frac{2\pi}{3}$

b) $y = 5 \sin \frac{1}{4}x$

Amp: 5
 Period: 8π

4) Graph the function.

$y = \sin(x - \frac{\pi}{3})$

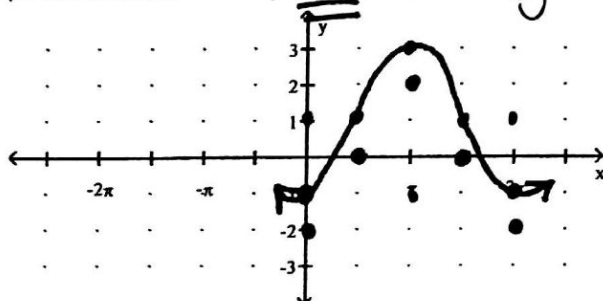


Amp: 1
 Period: 2π
 Phase Shift: $\frac{\pi}{3}$

5) Graph the function.

$y = 1 - 2 \cos x$

$y = -2 \cos(x + 1)$



Amp: 2
 Period: 2π
 Phase Shift: none
 Vertical Shift: up 1
 *reflect over x-axis